

Class: XII **THREE DIMENSIONAL GEOMETRY**

1. Find the equation of the plane passing through the points $(-1,2,0)$, $(2,2,-1)$ and parallel to the line $\frac{x-1}{1} = \frac{2y+1}{2} = \frac{z+1}{-1}$.
2. Find the equation of a plane passes through the point $(3,2,0)$ and contains the line $\frac{x-3}{1} = \frac{y-6}{5} = \frac{z-4}{4}$.
3. If lines $\frac{x-1}{2} = \frac{y+1}{3} = \frac{z-1}{4}$ and $\frac{x-3}{1} = \frac{y-k}{2} = \frac{z}{1}$ intersect, then find the value of k and hence find the equation of the plane containing these lines.
4. Find the distance of the point $P(3,4,4)$ from the point, where the line joining the points $A(3,-4,-5)$ and $B(2,-3,1)$ intersects the plane $2x+y+z=7$.
5. Find the distance of the point $(1,-2,3)$ from the plane $x - y + z = 5$ measured parallel to the line whose direction cosines are proportional to $2, 3, -6$.
6. Write the vector equation of the plane passing through the point (a,b,c) and parallel to the plane $\vec{r} \cdot (\vec{i} + \vec{j} + k) = 2$.
7. If the Cartesian equation of the line is $\frac{3-x}{5} = \frac{y+4}{7} = \frac{6z-4}{4}$, write the vector equation for the line.
8. Find a vector \vec{a} of magnitude $5\sqrt{2}$, making an angle of $\frac{\pi}{4}$ with x-axis, $\frac{\pi}{2}$ with y-axis and acute angle θ with z-axis.

9. Find the angle between the lines $\vec{r} = 2i - 5j + k + \lambda(3i + 2j + 6k)$ and $\vec{r} = 7i - 6k + \mu(i + 2j + 2k)$.
10. Show that the lines $\frac{x+1}{3} = \frac{y+3}{5} = \frac{z+5}{7}$ and $\frac{x-2}{1} = \frac{y-4}{3} = \frac{z-6}{5}$ intersect. Also find their point of intersection.
11. A line passes through (2, -1, 3) and is perpendicular to the lines $\vec{r} = (i + j - k) + \lambda(2i - 2j + k)$ and $\vec{r} = (2i - j - 3k) + \mu(i + 2j + 2k)$.
12. Find the value of p , so that the lines $l_1 : \frac{1-x}{3} = \frac{7y+14}{p} = \frac{z-3}{2}$ and $l_2 : \frac{7-7x}{3p} = \frac{y-5}{1} = \frac{6-z}{5}$ are perpendicular to each other. Also find the equations of a line passing through a point (3, 2, -4) and parallel to line l_1 .
13. Find the vector and Cartesian equations of the line passing through the point (2, 1, 3) and perpendicular to the lines $\frac{1-x}{-3} = \frac{y-2}{2} = \frac{z-3}{3}$ and $\frac{x}{-3} = \frac{y}{2} = \frac{z}{5}$.
14. Find the shortest distance between the lines whose vector equations are $\vec{r} = (i + j) + \lambda(2i - j + k)$ and $\vec{r} = (2i + j - k) + \mu(3i - 5j + 2k)$.
15. Find the equation of the plane that contains the point (1, -1, 2) and is perpendicular to both the planes $2x+3y-2z = 5$ and $x+2y-3z = 8$. Hence, find the distance of point P(-2, 5, 5) from the plane obtained above.
16. Find the distance of the point P(-1, -5, -10) from the point of intersection of the line joining the points A(2, -1, 2) and B(5, 3, 4) with the plane $x - y + z = 5$.
17. Find the distance between the point (7, 2, 4) and the plane determined by the points A(2, 5, -3), B(-2, -3, 5) and C(5, 3, -3).

18. Find the distance between the lines: $\frac{x+1}{7} = \frac{y+1}{-6} = \frac{z+1}{1}$;
 $\frac{x-3}{1} = \frac{y-5}{-2} = \frac{z-7}{1}$.
19. Find the distance of the point (-1, -5, -10) from the point of intersection of the line $\vec{r} = (2i - j + 2k) + \lambda(3i + 4j + 2k)$ and the plane $\vec{r} \cdot (i + j + k) = 5$.
20. Show that the lines $\frac{5-x}{-4} = \frac{y-7}{4} = \frac{z+3}{-5}$ and $\frac{x-8}{7} = \frac{2y-8}{2} = \frac{z-5}{3}$ are coplanar.
21. Show that the lines $\vec{r} = (i + j - k) + \lambda(3i - j)$ and $\vec{r} = (4i - k) + \mu(2i + 3k)$ intersect. Also find their point of intersection.
22. Find the equation of the plane through the line of intersection of the planes $x + y + z = 1$ and $2x + 3y + 4z = 5$ which is perpendicular to the plane $x - y + z = 0$. Also find the distance of the plane obtained above from the origin.
23. Find the distance of the point (2, 12, 5) from the point of intersection of the line $\vec{r} = (2i - 4j + 2k) + \lambda(3i + 4j + 2k)$ and the plane $\vec{r} \cdot (i - 2j + k) = 0$
24. Find the distance between the lines l_1 and l_2 given by
 $l_1 : \vec{r} = (i + 2j - 4k) + \lambda(2i + 3j + 6k)$;
 $l_2 : \vec{r} = (3i + 3j - 5k) + \mu(4i + 6j + 12k)$.
25. If a unit vector \vec{a} makes angles $\frac{\pi}{3}$ with \vec{i} , $\frac{\pi}{4}$ with \vec{j} and an acute angle θ with \vec{k} , then find the value of θ .
26. Find the length of the perpendicular drawn from the origin to the plane $2x - 3y + 6z + 21 = 0$.

27. Write the Cartesian equation of a plane, bisecting the line segment joining the points A(2, 3, 5) and B(4, 5, 7) at right angles.
28. Find the coordinates of the point, where the line $\frac{x-2}{3} = \frac{y+1}{4} = \frac{z-2}{2}$ intersects the plane $x - y + z = 5$. Also find the angle between the line and the plane.
29. Find the vector equation of the plane which contains the line of intersection of the planes $\vec{r} \cdot (i + 2j + 3k) - 4 = 0$ and $\vec{r} \cdot (2i + j - k) + 5 = 0$ and which is perpendicular to the plane $\vec{r} \cdot (5i + 3j - 6k) + 8 = 0$.
30. Show that the lines $\vec{r} = (3i + 2j - 4k) + \lambda(i + 2j + 2k)$; $\vec{r} = (5i - 2j) + \mu(3i + 2j + 6k)$ are intersecting. Hence find their point of intersection.
31. Find the vector equation of the plane through the points (2, 1, -1) and (-1, 3, 4) and perpendicular to the plane $x - 2y + 4z = 10$.
32. Find the vector equation of the plane passing through three points with position vectors $i + j - 2k$; $2i - j + k$ and $i + 2j + k$. Also find the coordinates of the point of intersection of this plane and the line $\vec{r} = (3i - j - k) + \lambda(2i - 2j + k)$.
33. Find the vector equation of the plane determined by the points A(3, -1, 2), B(5, 2, 4) and C(-1, -1, 6). Also find the distance of point P(6, 5, 9) from this plane.
34. Find the coordinates of the point where the line through (3, -4, -5) and (2, -3, 1) crosses the plane, passing through the points (2, 2, 1) and (3, 0, 1) and (4, -1, 0).
35. Find the equation of the plane passing through the line of intersection of the planes $\vec{r} \cdot (i + 3j) - 6 = 0$ and $\vec{r} \cdot (3i - j - 4k) = 0$, whose perpendicular distance from origin is unity.
36. Find the vector equation of the line passing through the point (1, 2, 3) and parallel to the planes $\vec{r} \cdot (i - j + 2k) = 5$ and $\vec{r} \cdot (3i + j + k) = 6$
37. Find the image of the point having position vector $i + 3j + 4k$ in the plane $\vec{r} \cdot (2i - j + k) + 3 = 0$.

38. Find the equation of the plane which is at a distance of $3\sqrt{3}$ units from origin and the normal to which is equally inclined to the coordinate axes.
39. If a line has direction ratios 2, -1, -2, then what are its direction cosines?
40. Find the distance of the plane $3x - 4y + 12z = 3$ from the origin.
41. Find the vector and Cartesian equation of the line passing through the point (1, 2, -4) and perpendicular to the two lines $\frac{x-8}{3} = \frac{y+19}{-16} = \frac{z-10}{7}$ and $\frac{x-15}{3} = \frac{y-29}{8} = \frac{z-5}{-5}$.
42. Find the equation of a line passing through the point P(2, -1, 3) and perpendicular to the lines $\vec{r} = (i + j - k) + \lambda(2i - 2j + k)$ and $\vec{r} = (2i - j - 3k) + \mu(i + 2j + 2k)$.
43. Find the equation of the line passing through the point (-1, 3, -2) and perpendicular to the lines $\frac{x}{1} = \frac{y}{2} = \frac{z}{3}$ and $\frac{x+2}{-3} = \frac{y-1}{2} = \frac{z+1}{5}$.
44. Find the coordinates of the point where the line through the points A(3, 4, 1) and B(5, 1, 6) crosses the XY-plane.
45. Find the coordinates of the point where the line through the points (3, -4, -5) and (2, -3, 1) crosses the plane $2x + y + z = 7$.
46. Find the coordinates of the point where the line through the points (3, -4, -5) and (2, -3, 1) crosses the plane $3x + 2y + z + 14 = 0$.
47. Find the vector and Cartesian equation of the line passes through the point (1, 2, 3) and parallel to the planes $\vec{r} \cdot (i - j + 2k) = 5$ and $\vec{r} \cdot (3i + j + k) = 6$.
48. Find the equation of the plane determined by the points A(3, -1, 2), B(5, 2, 4) and C(-1, -1, 6) and hence find the distance between the plane and the point P(6, 5, 9).
49. Find the length and the foot of the perpendicular from the point P(7, 14, 5) to the plane $2x + 4y - z = 2$. Also find the image of point P in the plane.

50. Find the coordinates of the foot of perpendicular and the length of the perpendicular drawn from the point $P(5, 4, 2)$ to the line $\vec{r} = (-i + 3j + k) + \lambda(2i + 3j - k)$. Also find the image of P in this line.
51. If a line makes angles $90^\circ, 60^\circ$ and θ with x, y and z axes respectively, where θ is acute, then find θ .
52. The equations of a line are $5x - 3 = 15y + 7 = 3 - 10z$. Write the direction cosines of the line.
53. Find the sum of the intercepts cut off by the plane $2x + y - z = 5$, on the coordinate axes.
54. Find the distance between the point $(-1, -5, -10)$ and the point of intersection of the line $\frac{x-2}{3} = \frac{y+1}{4} = \frac{z-2}{12}$ and the plane $x - y + z = 5$.
55. Find the equation of a line passing through the point $(1, 2, 4)$ and perpendicular to two lines $\vec{r} = (8\vec{i} - 19\vec{j} + 10\vec{k}) + \lambda(3\vec{i} - 16\vec{j} + 7\vec{k})$ and $\vec{r} = (15\vec{i} + 29\vec{j} + 5\vec{k}) + \mu(3\vec{i} + 8\vec{j} - 5\vec{k})$